Are there any monuments of Union soldiers in the American South?

-Blake Smith

There are literally thousands. I'm not going to make you a super long list, but take Vicksburg National Military Park for example. Every single state that contributed troops during the Civil War has a monument to their soldiers within the park.

I personally like the Illinois Monument...

While each state has an individual memorial to answer your question, yes there are monuments to Union troops in the South. Using Vicksburg as an example again here is the Memorial to African-American soldiers of the Civil War.
Here's the Monument to African-American Troops in Nashville
Even in my home state of Alabama, arguably portrayed as racist, backwards, and forever confederate, we have monuments that honor both the Northern troops and Southern troops.
The Iowa State Monument is located on Chickamauga Avenue in Rossville, Ga. The monument is dedicated to the men of Iowa in recognition of their service during the Battle of Missionary Ridge, fought Nov. 25, 1863, and is part of the Chickamauga and Chattanooga National Military Park.